

Final Exam Spring 1996

Bread-and-Butter Edition

An advantage of the general linear model approach or the neoclassical approach used in Judd & McClelland (1989) is the ability to generate and test complex models which ask sophisticated questions of data. However, we should not forget that the approach also facilitates the basic analyses used in many social science studies. This final exam focuses on those basic analyses and serves as a final review of the general linear model approach applied to bread-and-butter analyses.

Question 1

In this study of memory, there are two independent variables: subject mood and emotionality of words. Subjects are randomly assigned to one of 3 mood conditions: sad, neutral, or pleasant. To induce these moods the experiment has the subjects read a series of statements that are either sad, neutral, or pleasant, respectively. Within each mood condition, subjects are further randomly divided into groups asked to memorize either emotional words (such as "love" and "hate") or unemotional words (such as "shoe" and "tree"). The dependent variable is the number of words recalled on a test administered 30 minutes later. There are 18 subjects in this 3 x 2 design. [based on Glenberg (1988), p. 382]

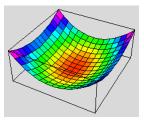
A. Your advisor asks you to do a two-way ANOVA. Specify the SAS commands you would use to do the analysis using contrasts.

B. Layout the source table, being sure to include rows for all main effects, interactions, and appropriate one-df tests. Fill in the df column.

Question 2

[from Kirk (1982), p. 565]. The performance of fifteen clerks on three date-sorting tasks was compared at two times of day: 10 A.M. and 4 P.M. Each clerk completed the date-sorting tasks at each time, but on different days (with the order of the times randomly determined). The task involved





sorting a list of random dates written in European form (e.g., 30 1 74 for January 30, 1974). Clerks were randomly assigned to sort the dates into either two, three, or four accounting periods. The dependent variable was the number of dates sorted in a fixed time. (Experiment suggested by Monk, T.H., & Conrad, M.C. (1979). Time of day effects in a range of clerical tasks. Human Factors, 21, 191-194).

A. Using the SAS input and output below, construct a complete source table.

B. Write a brief summary of the results.

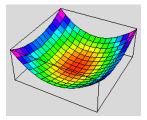
C. The periods variable is numeric so instead of using contrast codes, we could have used the SAS command:

```
proc glm;
btwn: model w0 = periods periods*periods;
wthn: model w1 = periods periods*periods;
```

Put a star, check, or other mark by the rows in your source table which would be different if the above SAS code had been used instead of the proc reg commands which were used in the output below.

```
data clerks;
   input subj periods am pm;
   w0 = (am + pm)/sqrt(2);
   w1 = (am - pm)/sqrt(2);
   lin = (1/2)*(periods=2) + 0*(periods=3) - (1/2)*(periods=4);
   quad = (-1/3)*(periods=2) + (2/3)*(periods=3)-(1/3)*(periods=4);
   label w0 = "Combined Score am + pm"
          w1 = "Difference Score am - pm"
          lin = "linear effect of periods"
          quad = "quadratic effect of periods";
cards;
 1 2 171 189
 2 2 183 204
 3 2 145 154
 4 2 158 166
 5 2 196 179
 6 3 213 249
 7 3 224 237
 8 3 198 224
 9 3 182 198
10 3 172 214
11 4 200 212
12 4 226 224
13 4 213 196
```

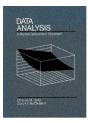


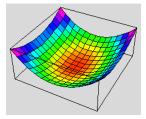


14 4 251 259 15 4 238 239 ;; proc reg; btwn: model w0 = lin quad/ss2; wthn: model w1 = lin quad/ss2;

The SAS System

Model: BTWN Dependent Variable: W0 Combined Score am + pm Analysis of Variance Sum of Mean Source DF Squares Square F Value Prob>F Model 2 13957.80000 6978.90000 8.821 0.0044 12 9494.00000 791.16667 Error 14 23451.80000 C Total Root MSE 28.12769 R-square 0.5952 Dep Mean 288.21672 Adj R-sq 0.5277 C.V. 9.75921 Parameter Estimates Parameter Standard T for H0: Variable DF Estimate Parameter=0 Prob > |T|Error INTERCEP 1 288.216724 7.26253705 39.685 0.0001 -72.549156 LIN 1 17.78951002 -4.078 0.0015 QUAD 1 15.485639 15.40616760 1.005 0.3347 Squared Partial Variable DF Type II SS Corr Type II INTERCEP 1 1246033 LIN 1 13158 0.58088419 1 799.350000 0.07765693 QUAD Variable Label Variable DF INTERCEP 1 Intercept LIN 1 linear effect of periods QUAD 1 quadratic effect of periods





The SAS System

Model: WTHN

Dependent Variable: W1 Difference Score am - pm

Analysis of Variance

Source	DF	Sum of Squares		F Value	Prob>F
Model Error C Total	2 12 14	912.20000 1009.60000 1921.80000	84.13333	5.421	0.0210
Root MSE	0	9.17242	R-square	0.4747	

ROOC FIDE	· · · / 2 12	IC DYUULC	0.1/1/
Dep Mean	-8.20244	Adj R-sq	0.3871
C.V.	-111.82555		

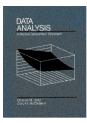
Parameter Estimates

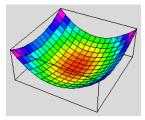
Variable	DF	Parameter Estimate	Standard Error	T for HO: Parameter=0	Prob > T
INTERCEP LIN QUAD	1 1 1	-8.202439 -5.232590 -15.909903	2.36830929 5.80114931 5.02394267	-3.463 -0.902 -3.167	0.0047 0.3848 0.0081
Variable	DF	Type II SS	Squared Partial Corr Type II		

INTERCEP	1	1009.200000	
LIN	1	68.450000	0.06349427
QUAD	1	843.750000	0.45525670

Variable Variable DF Label

INTERCEP	1	Intercept
LIN	1	linear effect of periods
QUAD	1	quadratic effect of periods





Question 3

[And now a problem for our students from business; from Neter, Wasserman, & Kutner (1983), p. 330]

An economist was interested in the speed with which a particular insurance innovation was adopted. Of particular interest was whether stock companies adopted innovations slower or faster than mutual companies. Also available was information on the size of the company (in millions of dollars of insurance policies in force). Relevant SAS input commands and output follow the questions.

A. Without controlling for size of firm, is there a difference between the time to adopt the innovation for mutual as compared to stock companies? Give the appropriate PRE, F*, and p.

B. Using ANCOVA, is there a difference between the time to adopt the innovation for mutual as compared to stock companies when controlling for size of firm? Give the appropriate PRE, F*, and p. Give the adjusted means that are compared in this analysis.

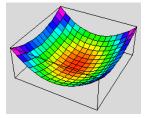
C. Explain in non-technical terms, such as in a memo to a CEO, why questions A and B have different answers.

D. Is there any evidence for a violation of the heterogeneity of regression assumption? Give the appropriate PRE, F*, and p.

E. Is the relationship between size and time to adopt the innovation different for mutual and stock companies? Give the appropriate PRE, F*, and p.

```
data firms;
   input time size type$;
   MvsS = (1/2)*(type="Mutual") - (1/2)*(type="Stock");
   SizeMvsS = size * MvsS;
   label time = "Months to Adopt"
          size = "Size of Firm ($1,000,000s)"
          MvsS = "Mutual vs. Stock Contrast"
         SizeMvsS ="Size by Mutual vs. Stock Interaction";
cards;
17 151 Mutual
26 92 Mutual
21 175 Mutual
30 31 Mutual
22 104 Mutual
0 277 Mutual
12 210 Mutual
```



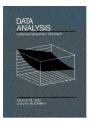


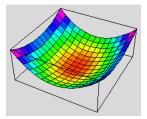
```
19 120 Mutual
4 290 Mutual
16 238 Mutual
28 164 Stock
15 272 Stock
11 295 Stock
38 68 Stock
31 85 Stock
21 224 Stock
20 166 Stock
13 305 Stock
30 124 Stock
14 246 Stock
;;
proc means;
  var time size;
  by type;
proc reg; title 'Simple Comparison';
  model time = MvsS;
proc reg; title 'ANCOVA Comparison';
  model time = MvsS size/ss2 pcorr2 tol;
  output out=temp h=lever r=resid p=timehat rstudent=rstudent
        cookd=cookd;
proc reg data=firms; title2 'with Interaction Added';
  model time = MvsS size SizeMvsS/ss2 pcorr2 tol;
The SAS System
TYPE=Mutual
                         N Mean Std Dev
Variable Label
______
                      10 16.7000000 9.2981480
TIME Months to Adopt
      Size of Firm ($1,000,000s) 10 168.8000000 84.7909848
SIZE
_____
                                Minimum Maximum
Variable Label
_____

        TIME
        Months to Adopt
        0
        30.000000

        SIZE
        Size of Firm ($1,000,000s)
        31.0000000
        290.0000000

_____
TYPE=Stock
                         N Mean Std Dev
Variable Label
_____
TIMEMonths to Adopt1022.10000009.1706052SIZESize of Firm ($1,000,000s)10194.900000085.9863684
_____
                                Minimum Maximum
Variable Label
_____
TIMEMonths to Adopt11.00000038.000000SIZESize of Firm ($1,000,000s)68.000000305.0000000
```





Simple Comparison Model: MODEL1 Dependent Variable: TIME Months to Adopt

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Prob>F
Model Error C Total	1 18 19	145.80000 1535.00000 1680.80000	145.80000 85.27778	1.710	0.2075

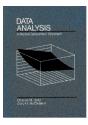
Root MSE	9.23460	R-square	0.0867
Dep Mean	19.40000	Adj R-sq	0.0360
C.V.	47.60101		

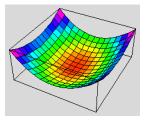
Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	T for HO: Parameter=O	Prob > T
INTERCEP MVSS	1 1	19.400000 -5.400000	2.06491862 4.12983723	9.395 -1.308	0.0001 0.2075
		Variable			

Variable DF Label

INTERCEP	1	Interce	ept		
MVSS	1	Mutual	vs.	Stock	Contrast





ANCOVA Comparison Model: MODEL1 Dependent Variable: TIME

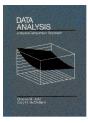
Months to Adopt

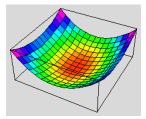
Analysis of Variance

Source	DF	Sum c Square		F Value	Prob>F
Model Error C Total	2 17 19	1504.4133 176.3866 1680.8000	10.37569	72.497	0.0001
Root MSE Dep Mean C.V.	19	3.22113 9.40000 5.60377	R-square Adj R-sq	0.8951 0.8827	

Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	T for HO: Parameter=0	Prob > T
INTERCEP MVSS SIZE	1 1 1	37.901804 -8.055469 -0.101742	1.77004130 1.45910570 0.00889122	21.413 -5.521 -11.443	0.0001 0.0001 0.0001
Variable	DF	Type II SS	Squared Partial Corr Type II	Tolerance	
INTERCEP MVSS SIZE	1 1 1	4757.401281 316.245973 1358.613335	0.64195091 0.88509012	0.97470527 0.97470527	
Variable	DF	Variable Label			
INTERCEP MVSS SIZE	1 1 1	Intercept Mutual vs. St Size of Firm			





ANCOVA Comparison with Interaction Added

Model: MODEL1 Dependent Variable: TIME Months to Adopt

17.11450

Analysis of Variance

Source	DF	Sum Squa	-	Mean Square	F Value	Prob>F
Model Error C Total	3 16 19	1504.419 176.380 1680.800	096	501.47301 11.02381	45.490	0.0001
Root MSE Dep Mean	19	3.32021 9.40000		square j R-sq	0.8951 0.8754	

Parameter Estimates

C.V.

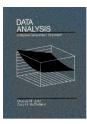
Variable	DF	Parameter Estimate	Standard Error	T for HO: Parameter=0	Prob > T
INTERCEP	1	37.903995	1.82702585	20.746	0.0001
MVSS	1	-8.131250	3.65405169	-2.225	0.0408
SIZE	1	-0.101739	0.00916561	-11.100	0.0001
SIZEMVSS	1	0.000417	0.01833121	0.023	0.9821

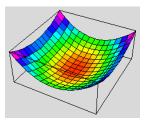
Variable	DF	Type II SS	Squared Partial Corr Type II	Tolerance
INTERCEP	1	4744.738605		
MVSS	1	54.587974	0.23634336	0.16512481
SIZE	1	1358.269138	0.88506764	0.97451427
SIZEMVSS	1	0.005708	0.00003236	0.16555219

Variable

Variable	DF	Label
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INTERCEP	1	Intercept
MVSS	1	Mutual vs. Stock Contrast
SIZE	1	Size of Firm (\$1,000,000s)
SIZEMVSS	1	Size by Mutual vs. Stock Interaction





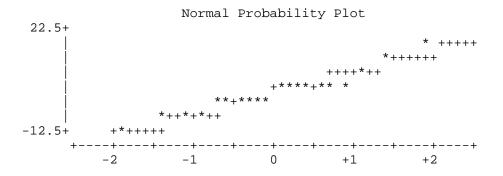
F. The following SAS output of residuals and plots was for a preliminary analysis like the one above. Comment on how well the assumptions were satisfied for this preliminary analysis and comment on any outliers. What next step would you recommend?

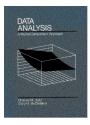
ANCOVA Comparison									
OBS	MVSS	SIZE	SIZEMVSS	TIME	TIMEHAT	RESID	LEVER	RSTUDENT	COOKD
1	0.5	151	75.5	17	19.0997	-2.0997	0.11192	-0.27543	0.00337
2	0.5	92	46.0	26	21.5492	4.4508	0.14869	0.60159	0.02189
3	0.5	575	287.5	21	1.4964	19.5036	0.57858	9.83323	6.67537
4	0.5	31	15.5	30	24.0818	5.9182	0.21282	0.84060	0.06480
5	0.5	104	52.0	22	21.0510	0.9490	0.13920	0.12620	0.00091
б	0.5	277	138.5	0	13.8685	-13.8685	0.11660	-2.04340	0.15479
7	0.5	210	105.0	12	16.6502	-4.6502	0.10001	-0.61153	0.01438
8	0.5	120	60.0	19	20.3867	-1.3867	0.12814	-0.18335	0.00175
9	0.5	290	145.0	4	13.3288	-9.3288	0.12353	-1.29132	0.07538
10	0.5	238	119.0	16	15.4877	0.5123	0.10304	0.06672	0.00018
11	-0.5	164	-82.0	28	23.3829	4.6171	0.10341	0.60826	0.01477
12	-0.5	272	-136.0	15	18.8990	-3.8990	0.12121	-0.51721	0.01285
13	-0.5	295	-147.5	11	17.9441	-6.9441	0.13576	-0.94664	0.04721
14	-0.5	68	-34.0	38	27.3685	10.6315	0.15747	1.52923	0.13506
15	-0.5	85	-42.5	31	26.6628	4.3372	0.14310	0.58396	0.01975
16	-0.5	224	-112.0	21	20.8918	0.1082	0.10302	0.01408	0.00001
17	-0.5	166	-83.0	20	23.2998	-3.2998	0.10298	-0.43218	0.00751
18	-0.5	305	-152.5	13	17.5289	-4.5289	0.14326	-0.61041	0.02156
19	-0.5	124	-62.0	30	25.0436	4.9564	0.11794	0.65962	0.02006
20	-0.5	246	-123.0	14	19.9785	-5.9785	0.10932	-0.79657	0.02653

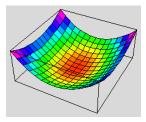
ANCOVA Comparison Normal-Normal Quantile Plot

Variable=RESID

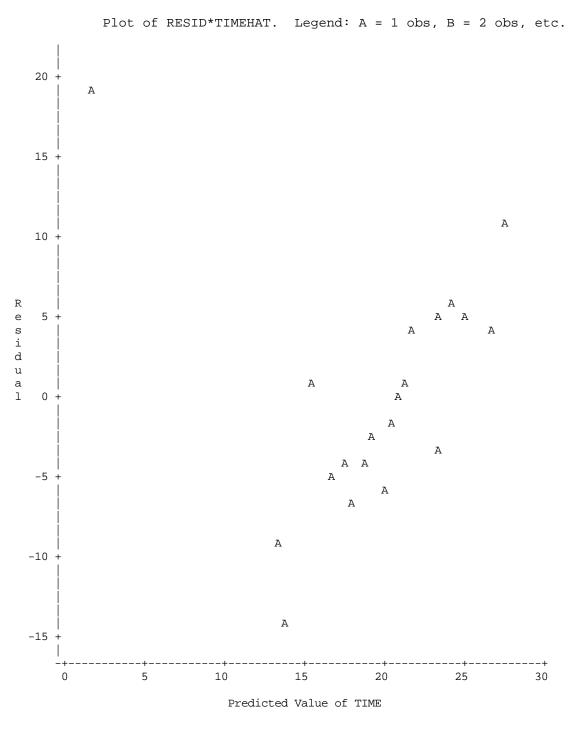
Residual

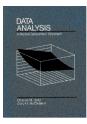


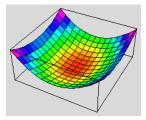




ANCOVA Comparison Plot of Residuals vs. Predicted







Question 4

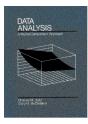
[also from Neter, et al., p. 364] In a study of the effectiveness of coupons offering a price reduction on a given product, 1000 homes were selected and a coupon and advertising material for the product were mailed to each. The coupons offered different price reductions (5, 10, 15, 20, and 30 percent) for specific automobile maintenance services; 200 homes were randomly assigned to each of the price reduction categories. The response variable was whether the coupon was redeemed within six months.

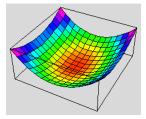
A. Is the price reduction percentage related to the rate at which coupons were redeemed? Give the appropriate test statistic and p.

B. Is there any evidence that the effectiveness of the price reduction did not increase linearly (in terms of logits)? Give the appropriate test statistic and p.

C. Your boss decides that a 25% price reduction is the most your firm can afford. What is the expected proportion of coupons that would be redeemed if a 25% reduction were offered?

-	-	pons; reduce count redeem; esq = reduce * reduce;			
card	ds;				
5	32	1			
5	168	0			
10	51	1			
10	149	0			
15	70	1			
15	130	0			
20	103	1			
20	97	0			
30	148	1			
30	52	0			
;;					
<pre>proc logistic; model redeem = reduce; weight count; proc logistic; model redeem = reduce reducesq; weight count;</pre>					





The LOGISTIC Procedure

Data Set: WORK.COUPONS Response Variable: REDEEM Response Levels: 2 Number of Observations: 10 Weight Variable: COUNT Sum of Weights: 1000 Link Function: Logit

Response Profile

Ordered Value	REDEEM	Count	Total Weight
1	0	5	596.00000
2	1	5	404.00000

Criteria for Assessing Model Fit

Criterion	Intercept Only	Intercept and Covariates	Chi-Square for Covariates
AIC	1351.200	1172.763	
SC	1351.503	1173.368	
-2 LOG L	1349.200	1168.763	180.437 with 1 DF (p=0.0001)
Score		•	173.057 with 1 DF (p=0.0001)

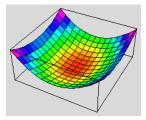
Analysis of Maximum Likelihood Estimates

Variable	DF	Parameter Estimate		Wald Chi-Square	Pr > Chi-Square	Standardized Estimate	Odds Ratio
INTERCPT	1	2.1855	0.1647	176.1542	0.0001		8.895
REDUCE	1	-0.1087	0.00884	151.1552	0.0001	-5.435146	0.897

Association of Predicted Probabilities and Observed Responses

Concordant	=	40.0%	Somers' D	=	0.000
Discordant	=	40.0%	Gamma	=	0.000
Tied	=	20.0%	Tau-a	=	0.000
(25 pairs)			C	=	0.500





The SAS System

The LOGISTIC Procedure

Data Set: WORK.COUPONS Response Variable: REDEEM Response Levels: 2 Number of Observations: 10 Weight Variable: COUNT Sum of Weights: 1000 Link Function: Logit

Response Profile

Ordered Value	REDEEM	Count	Total Weight
1	0	5	596.00000
2	1	5	404.00000

Criteria for Assessing Model Fit

Criterion	Intercept Only	Intercept and Covariates	Chi-Square for Covariates
AIC SC -2 LOG L	1351.200 1351.503 1349.200	1174.722 1175.629 1168.722	180.479 with 2 DF (p=0.0001)
Score	•	•	173.339 with 2 DF (p=0.0001)

Analysis of Maximum Likelihood Estimates

Variable D	Parameter F Estimate		Wald Chi-Square	Pr > Chi-Square	Standardized Estimate	Odds Ratio
INTERCPT 1	2.2428	0.3267	47.1399	0.0001		9.420
REDUCE 1	-0.1167	0.0400	8.5032	0.0035	-5.832308	0.890
REDUCESQ 1	0.00022	0.00108	0.0415	0.8385	0.398600	1.000

Association of Predicted Probabilities and Observed Responses

Concordant	=	40.0%	Somers' I) =	0.000
Discordant	=	40.0%	Gamma	=	0.000
Tied	=	20.0%	Tau-a	=	0.000
(25 pairs)			С	=	0.500