Psychophysical Scaling

Fechner's Law (Fechner, 1860)

R = unit of stimulus measurement (Reiz)

S = unit of subjective measurement

K, k, C and c are constants

(1)
$$\frac{\partial R}{R} = K$$
 (for and at the JND) E. H. Weber's Law

(2)
$$\partial S = c \cdot \frac{\partial R}{R}$$
 Fundamental formel

Integrate to get the magnitude of S (sensation)

$$(3) S = c \cdot \ln R + C$$

At threshold, S = 0, R = r, therefore: $0 = c \cdot \ln r + C$ or $C = -c \cdot \ln r$ Substituting this relationship into (3):

$$S = c \cdot \ln R - c \cdot \ln r$$
 or $S = c \cdot (\ln R - \ln r)$ or

$$(4) S = c \cdot \ln\left(\frac{R}{r}\right)$$

Converting Equation 4 from natural logarithms to base 10 logarithms

(5)
$$S = k \cdot \log\left(\frac{R}{r}\right)$$
 Massformel

Making r (the threshold stimulus value) the unit of R, we have:

(6)
$$S = k \cdot \log R$$
 Fechner's Law

Conditions for the validity of Fechner's Law:

- 1. Unit of R is r (threshold value)
- 2. Integration of Equation 2 is valid
- 3. Valid to assume that S = 0 at R = r
- 4. That Weber's Law is valid

Major Criticisms

- 1. All JNDs do not give rise to equal sensation magnitudes
- 2. Sensations don't only have magnitude, but also quality (e.g., color, pitch)

Lewis O. Harvey, Jr.–Instructor Clare Sims–Assistant MUEN D156, 09:30–10:45 TR

Stevens' Law (Stevens, 1936)

20 JND's above auditory threshold do not sound twice as loud as 10 JND's above threshold.

Prothetic Continua

$$S = k \cdot R^n$$

$$S = k \cdot (R - r)^n$$

$$\log S = \log k + n \cdot \log R$$

Stevens' Law

Metathetic Continua

$$S = k \cdot \log R$$

Fechner's Law

General Psychophysical Law (Norwich & Wong, 1997)

Both Fechner's Law and Stevens' Law can be viewed as special cases of a more general law based on information processing principles.

$$S = \frac{1}{2} \cdot k \cdot \ln(1 + \gamma \cdot R^n)$$

Complete Form

Note that when $\gamma \cdot R^n >> 1$ the complete form becomes

$$S = \frac{1}{2} \cdot k \cdot n \cdot \ln R + \frac{1}{2} \cdot k \cdot \ln \gamma$$

Equivalent to Fechner's Law

which is really Fechner's Law since $\frac{1}{2}kn$ and $\frac{1}{2}k\ln\gamma$ are constants. The Taylor series expansion of the complete form has a first-order term of

$$S = \frac{1}{2} \cdot k \cdot \gamma \cdot R^n$$

Equivalent to Stevens' Law

References

Fechner, G. T. (1860). *Elemente der Psychophysik*. Leipzig, Germany: Breitkopf and Härtel.

Norwich, K. H., & Wong, W. (1997). Unification of psychophysical phenomena: The complete form of Fechner's law. *Perception & Psychophysics*, 59(6), 929–940.

Stevens, S. S. (1936). A scale for the measurement of a psychological magnitude: loudness. *Psychological Review*, *43*, 405–416.